

Automorphisms, Connections, and Motivic Cohomology

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2.3 Adeles and Ideles

<https://math.stackexchange.com/questions/25090/whats-the-significance-of-tates-thesis/25125#25125> <https://math.stackexchange.com/questions/290847/what-do-ideles-and-adeles-look-like>

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